



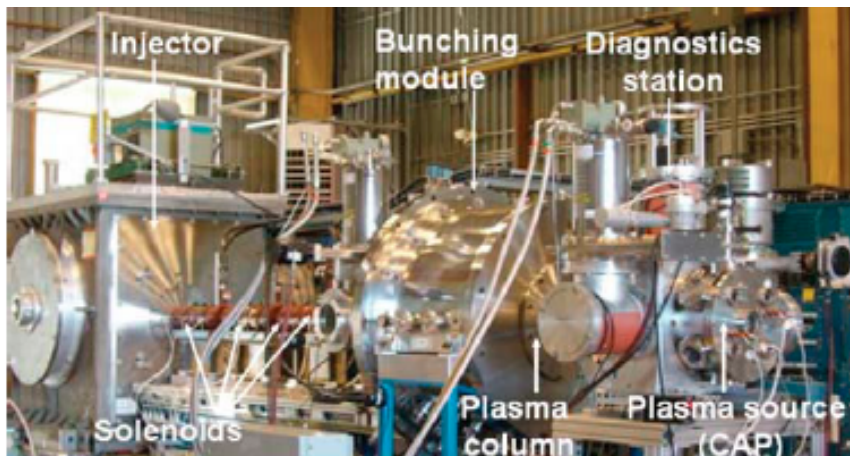
# Beam Physics for WDM

Warm Dense Matter Winter School

January 15, 2008

Jonathan Wurtele

UC Berkeley and LBNL

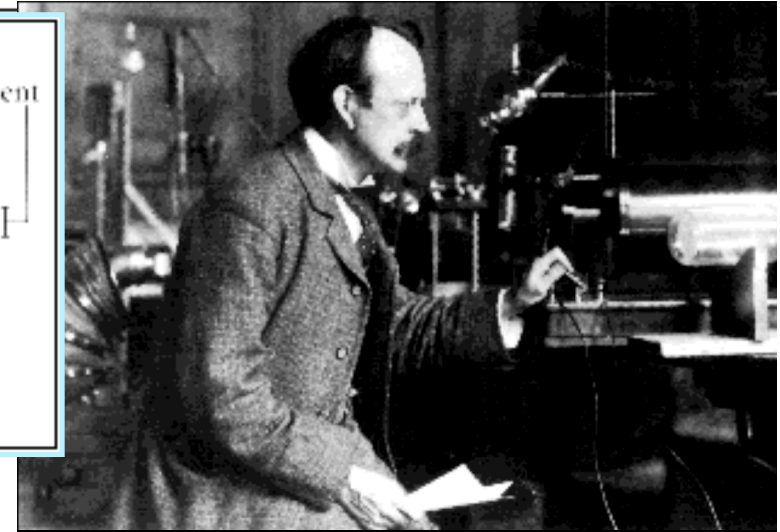
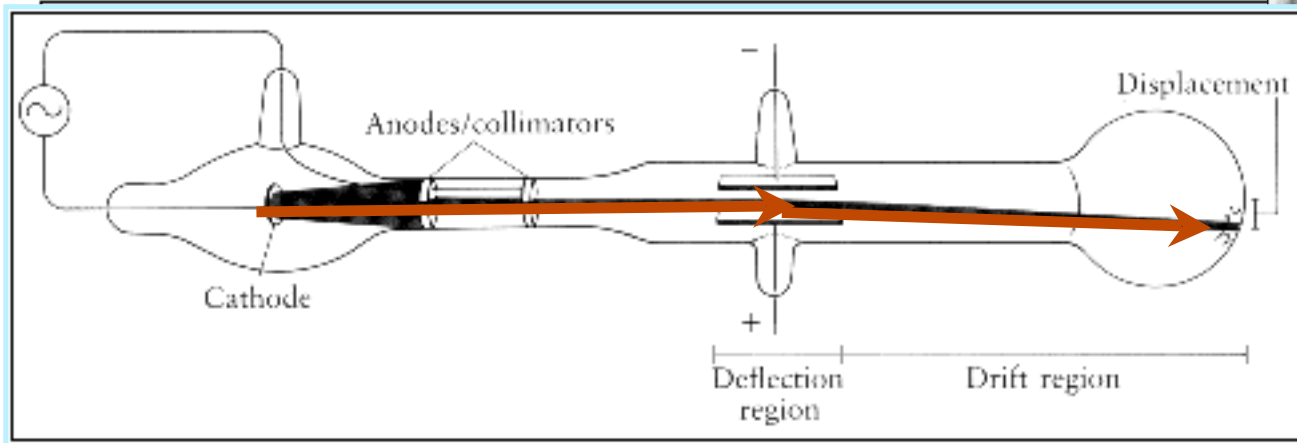


# How Accelerators Work

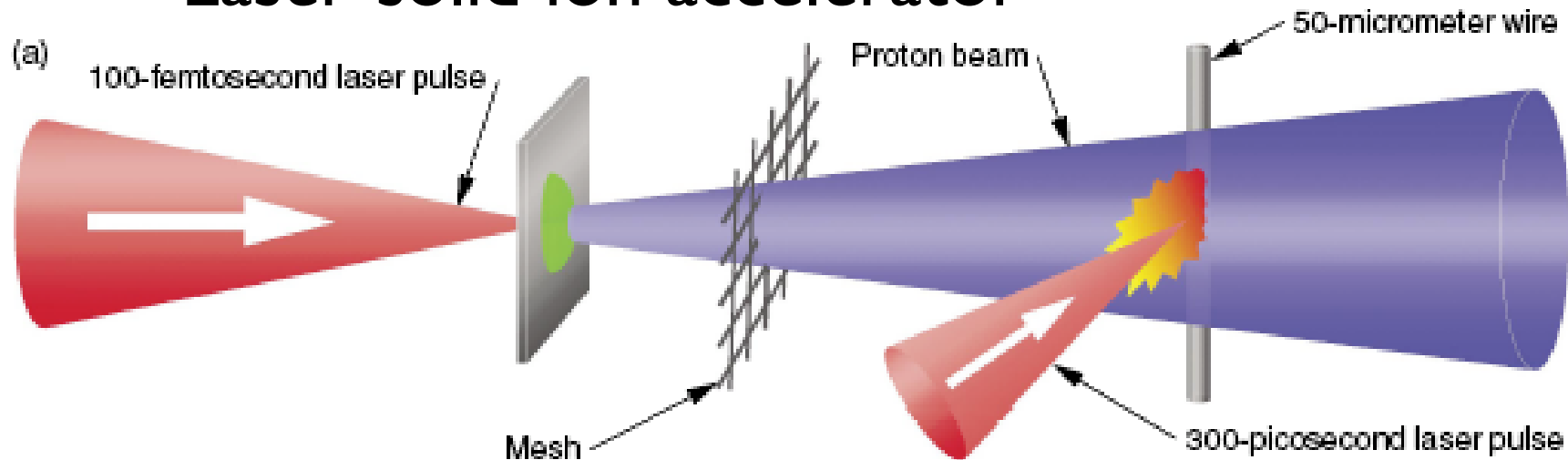
Magnetic and electric fields focus and deflect particles

Electric fields accelerate particles

J.J. Thomson: discovery of the electron



## Laser-solid ion accelerator



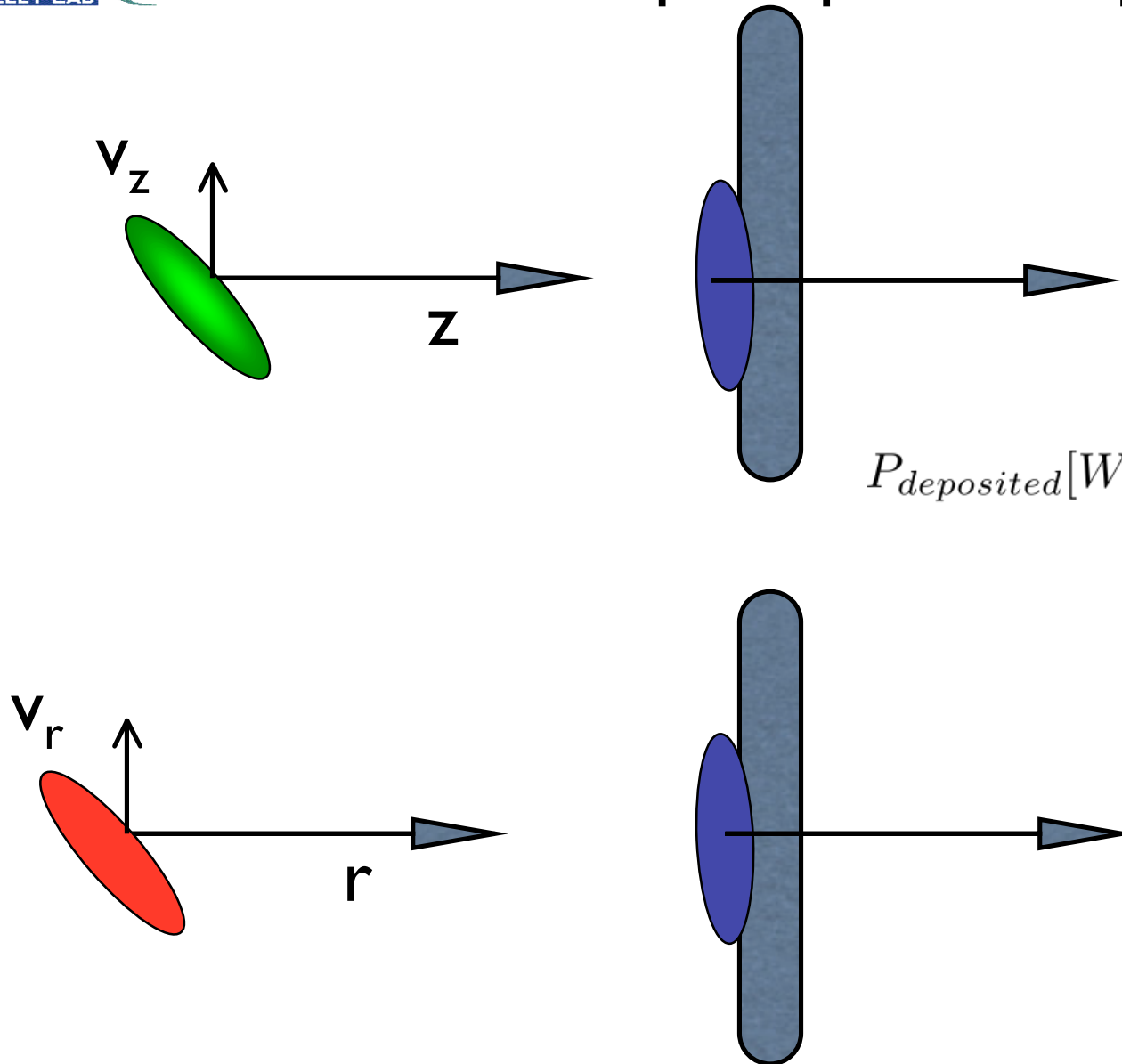


# Outline

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- Overview
- Ion beams
- Electron beams and X-ray FELs
- Plasma-based accelerators

# 3D focus for peak power deposition



$$\begin{aligned}
 P_{deposited}[W/kg] &= \frac{E_{deposited}}{\tau} \\
 &= \frac{(N_{ion} \frac{dE}{dz} L_{target})}{\tau \pi R_{beam}^2 L_{target} \rho_{tar}} \\
 &= \left( \frac{1}{\rho_t} \frac{dE}{dz} \right) \left( \frac{N_i}{\pi R_b^2 \tau} \right)
 \end{aligned}$$

Code: green is longitudinal phase space,  
red is transverse phase space, blue is r-z space



## The equations may be written in Lagrangian form

Convective derivative:

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \mathbf{v} \cdot \nabla$$

Mass conservation equation:

$$\frac{d\rho}{dt} = -\rho \nabla \cdot \mathbf{v}$$

Acceleration equation

$$\rho \frac{d\mathbf{v}}{dt} = -\nabla p$$

Adiabatic flow condition:

$$\rho \frac{ds}{dt} = \rho \dot{s}_{source}$$

In Lagrangian form, the energy conservation equation reads:

$$\frac{d}{dt} \left( \rho \epsilon + \frac{1}{2} \rho v^2 \right) = -\nabla \cdot (p \mathbf{v}) - \left( \rho \epsilon + \frac{1}{2} \rho v^2 \right) \nabla \cdot \mathbf{v} + \rho \dot{\epsilon}_{source}$$



# Beam Brightness

$$B_n = \frac{N}{V_{6d}}$$

$$\underbrace{V_{6d}}_{\text{6d phase space}} = \underbrace{\epsilon_{n\parallel}}_{\text{2d longitudinal phase space}} \underbrace{\epsilon_{n\perp}^2}_{\text{4d perpendicular phase space}}$$

6d phase space

2d longitudinal phase space

4d perpendicular phase space

$$\frac{N}{\pi R_b^2 \tau} \propto B_n \frac{\epsilon_{n\perp}}{\beta} \delta E$$

$$\begin{aligned} P_{\text{deposited}} [W/kg] &= \frac{E_{\text{deposited}}}{\tau} \\ &= \frac{(N_{\text{ion}} \frac{dE}{dz} L_{\text{target}})}{\tau \pi R_{\text{beam}}^2 L_{\text{target}} \rho_{\text{target}}} \\ &= \left( \frac{1}{\rho_t} \frac{dE}{dz} \right) \left( \frac{N_i}{\pi R_b^2 \tau} \right) \end{aligned}$$

*B is invariant (technology and physics limits)*

*B is focusing (technology)  
Energy spread limited by target,  
chromatic defocusing, etc*



A goal for beam drivers: heat target to  $\sim 1\text{ eV}$  quickly  
(little hydro expansion)

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Time scale set by  $L/v$  where  $L$  is target dimension

X-ray drivers can penetrate for bulk heating

Laser drivers are absorbed in a skin depth (at low power)

Desired laser energy/pulse is not (now) hard to obtain

Intense charged particle beams are hard to obtain  
Charged particle beams tend to self-destruct.



# Envelope Equation

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$R$ =radius of beam

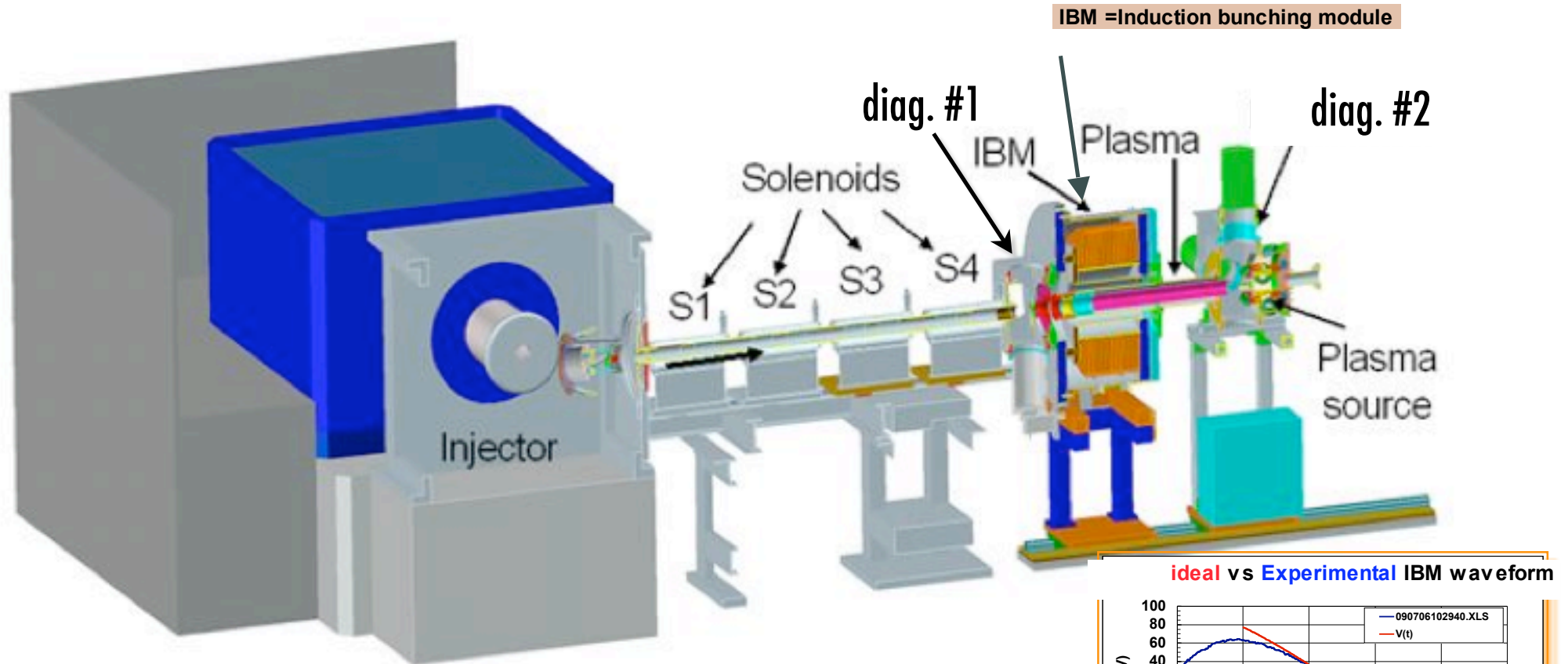
$$\frac{d^2 R}{dz^2} + \underbrace{\kappa^2 R}_{\text{focusing}} = \underbrace{\frac{I}{I_A \gamma^3 R}}_{\text{Space charge}} + \underbrace{\frac{\epsilon_{\perp}^2}{R^3 \gamma^2}}_{\text{pressure}}$$

Current neutralization eliminates (or reduces) space charge

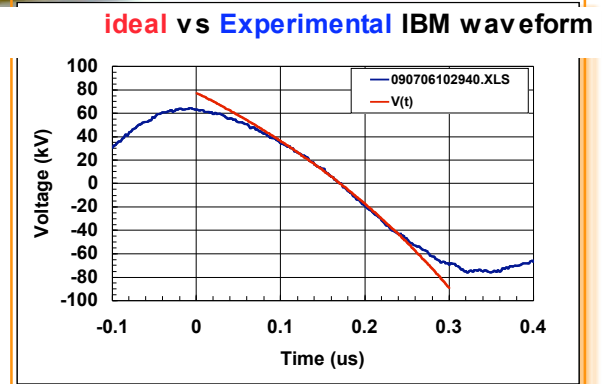
# Low energy ion driver experiment: simultaneous transverse focusing and longitudinal compression

P. Seidel, et al, APS DPP 2007

$E_i = 0.3 \text{ MeV K}^+$   
 $I_i = 25 \text{ mA}$

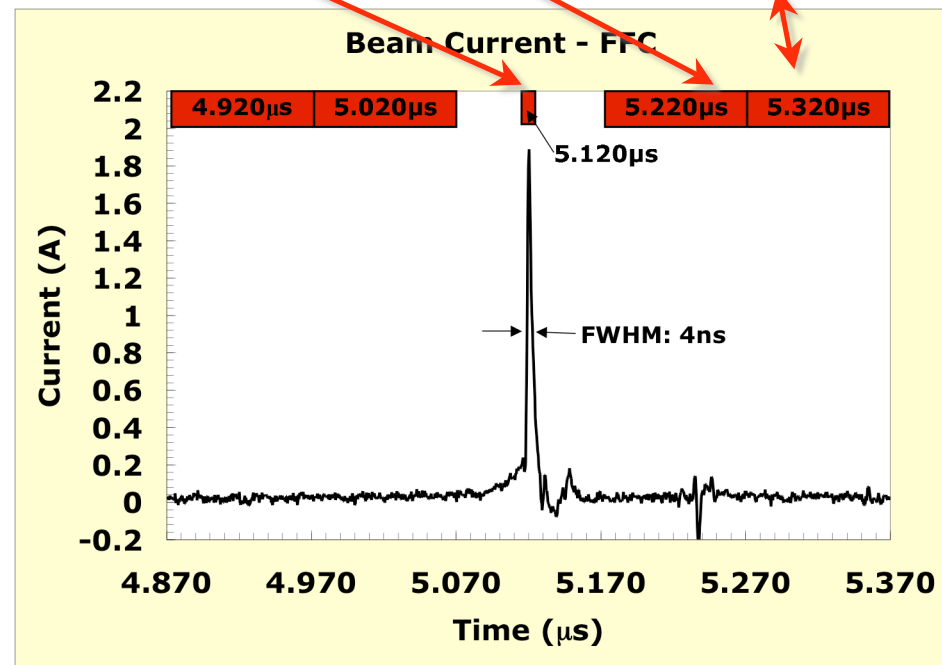
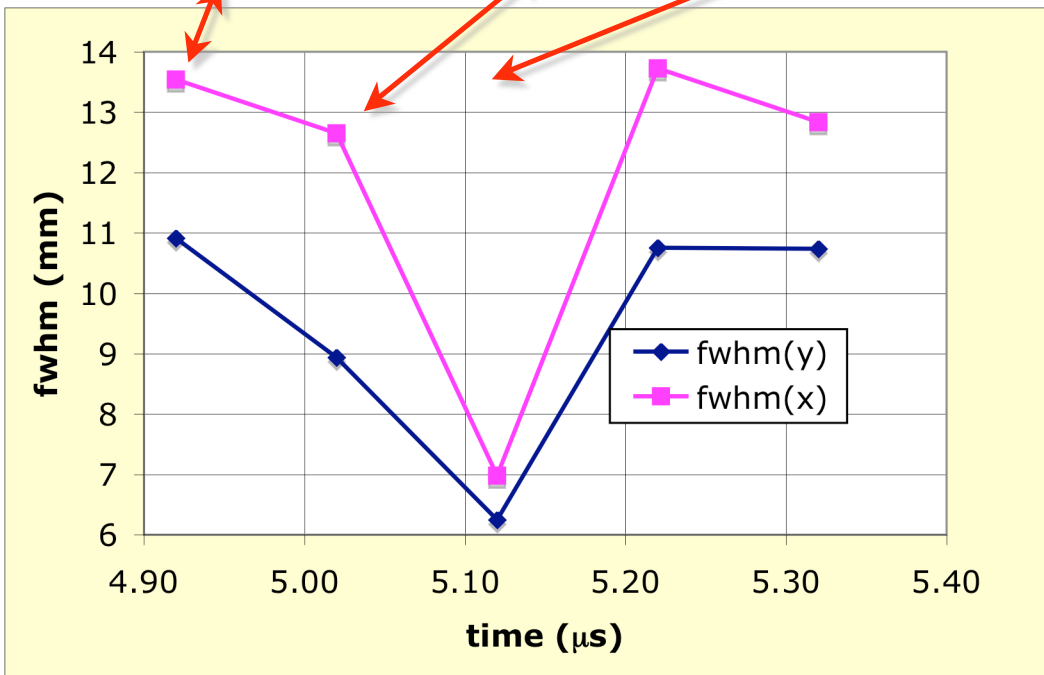
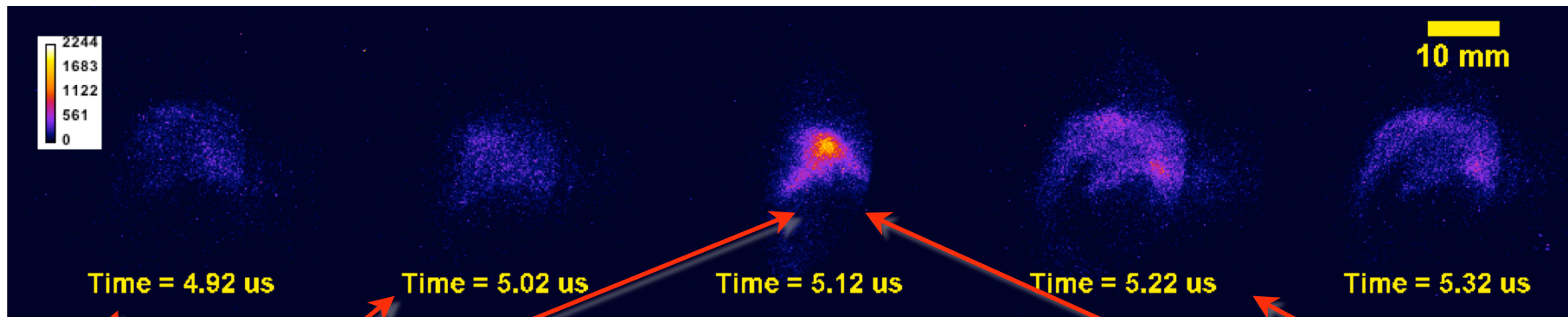


**Objectives:** Preservation of low emittance, plasma column with  $n_p > n_b$ ,  
 $(n_{b\text{-init}} \approx 10^9 / \text{cm}^3,$   
 $n_{b\text{max}} \approx 10^{12} / \text{cm}^3 \text{ now, later, } \approx 10^{13} / \text{cm}^3)$



# Minimum spot size @ same time as peak compression

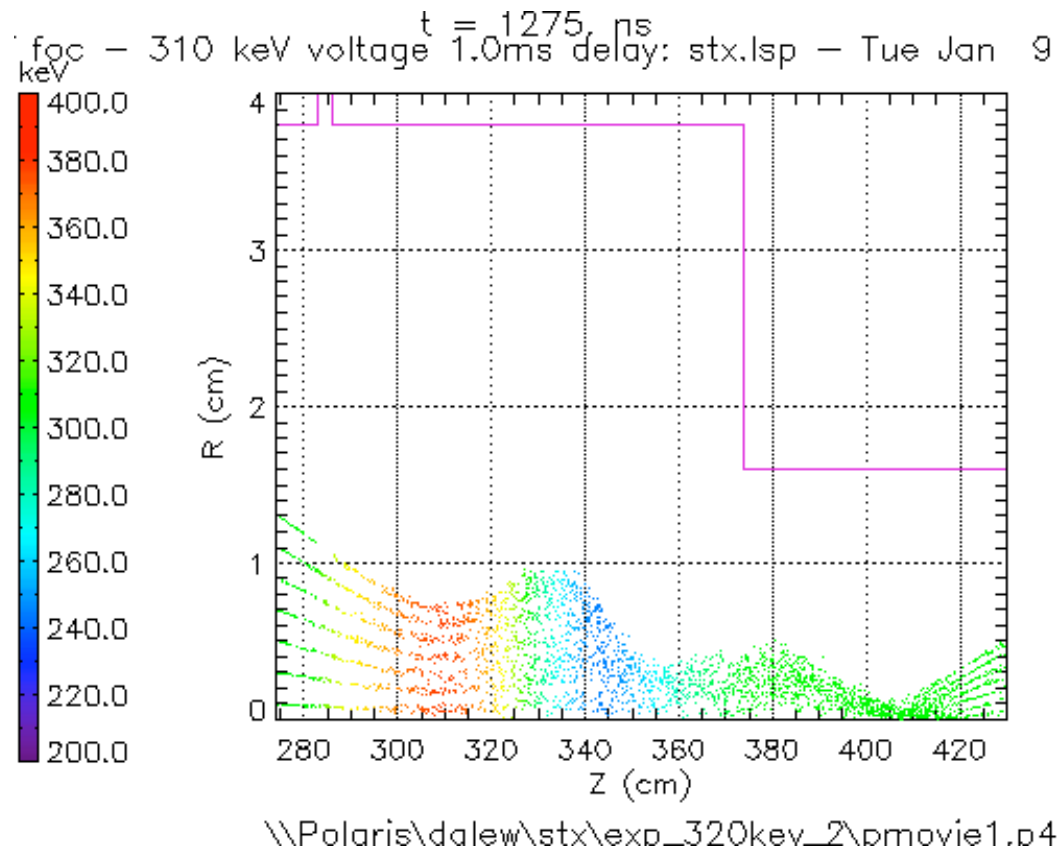
P. Seidel, et al, APS DPP 2007



2X reduction in the spot size (4X increase in beam intensity) brings the peak beam density to the range  $n_b \approx 10^{12} \text{ cm}^{-3}$ .



# LSP simulation (Welch, et al, 2007) of pulse compression on NDCX-I





# Ion driver parameters

Table 1. Neon beam:  $Z=10$ ,  $A=20.17$ ,  $E_{\min}=7.7$  MeV,  $E_{\text{center}}=12.1$  MeV,  $E_{\max}=20.1$  MeV, and  $\Delta z_{\min}=40$   $\mu$ .

$\rho(\text{g/cm}^3)\%$ solid	0.027 (1%)			0.27 (10%)			2.7 (100%)		
Foil length ( $\mu$ )	480			48			4.8		
kT (eV)	3.1	4.8	15	4.2	7.3	18	5.9	12	22
$Z^*$	1.1	2.1	2.7	0.56	1.7	2.6	0.56	1.2	2.5
$\Gamma_e=Z^{*2}e^2n_i^{1/3}/kT$	0.45	1.1	0.95	0.30	0.63	1.4	0.30	0.70	1.6
$N_{\text{core}}/(r_{\text{core}}/1\text{mm})^2/10^{12}$	1	3	10	1	3	10	1	3	10
$\Delta t$ (ns)	84	48	27	3.8	2.2	1.2	0.04	0.03	.014
$U$ (J/m <sup>3</sup> )/10 <sup>11</sup>	.015	.045	0.15	0.15	0.45	1.5	1.5	4.5	15

Barnard et al, PAC 2005

More parameters later today, esp. for ring geometry (Tahir)



# X-ray Free electron lasers

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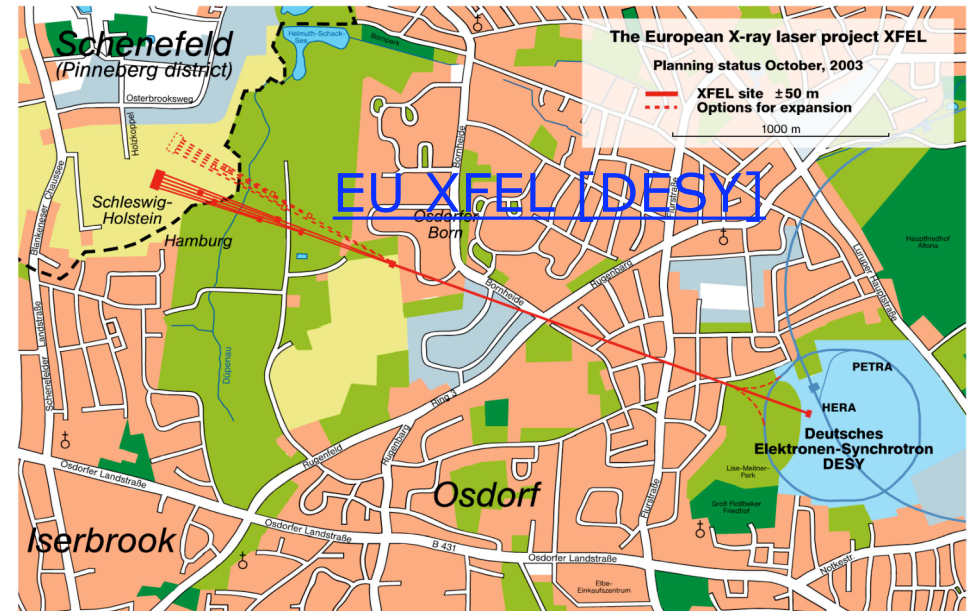
- 'Bulk' heating of matter with fs-ps x-rays pulses
- High intensity pulses driven by GeV electron beams
- FEL requires intense electron beam.  
Charged particle beams tend to self-destruct.

# X-ray sources expand

## JAPAN [SPRING 8]



Fig. 2 Proposed site for XFEL machine at SPring-8.

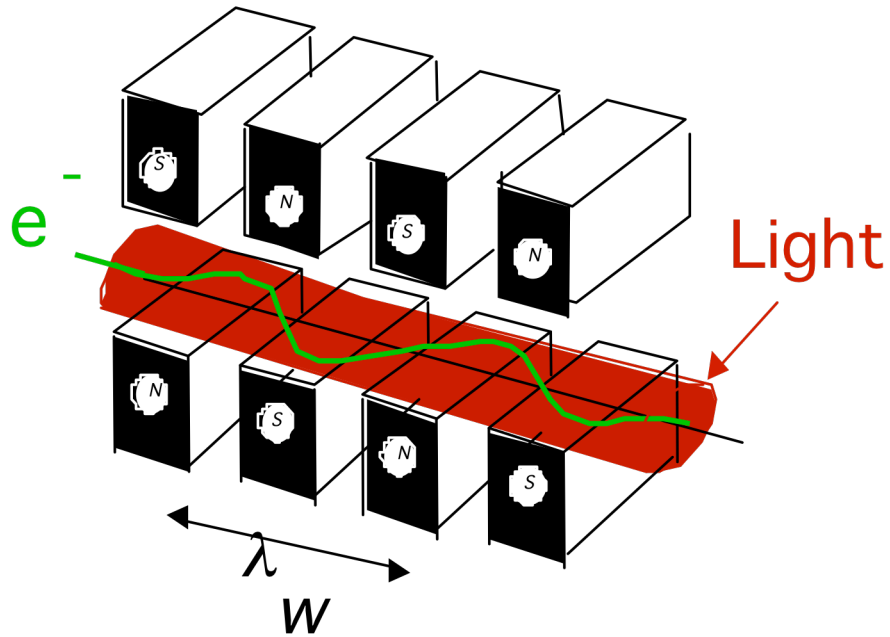


## LCLS [SLAC] FEL

Current	~3.5kA
Energy	~15GeV
Beam radius	~30microns
X-Ray Energy/pulse	~2.5mJ
Repetition rate	~120Hz



# X-ray Free Electron Laser

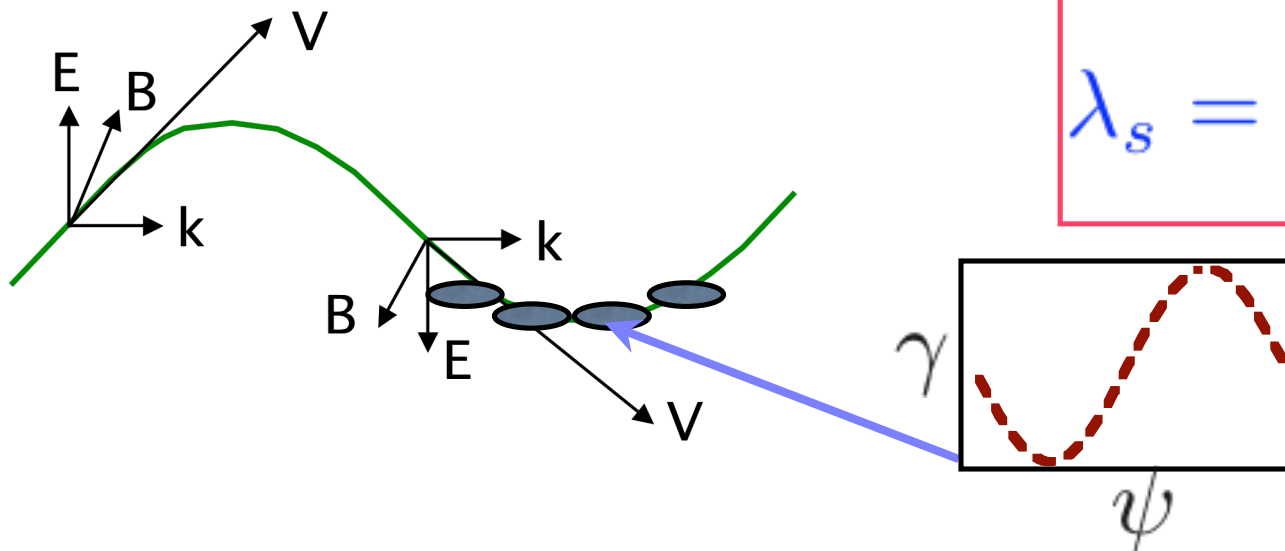


$$\frac{d\gamma}{dz} = \frac{q\vec{E} \cdot \vec{v}}{mc^2 v_z}$$

$$\psi = (k_s + k_w)z - \omega_s t$$

$$v_z = \frac{\omega_s}{k_s + k_w}$$

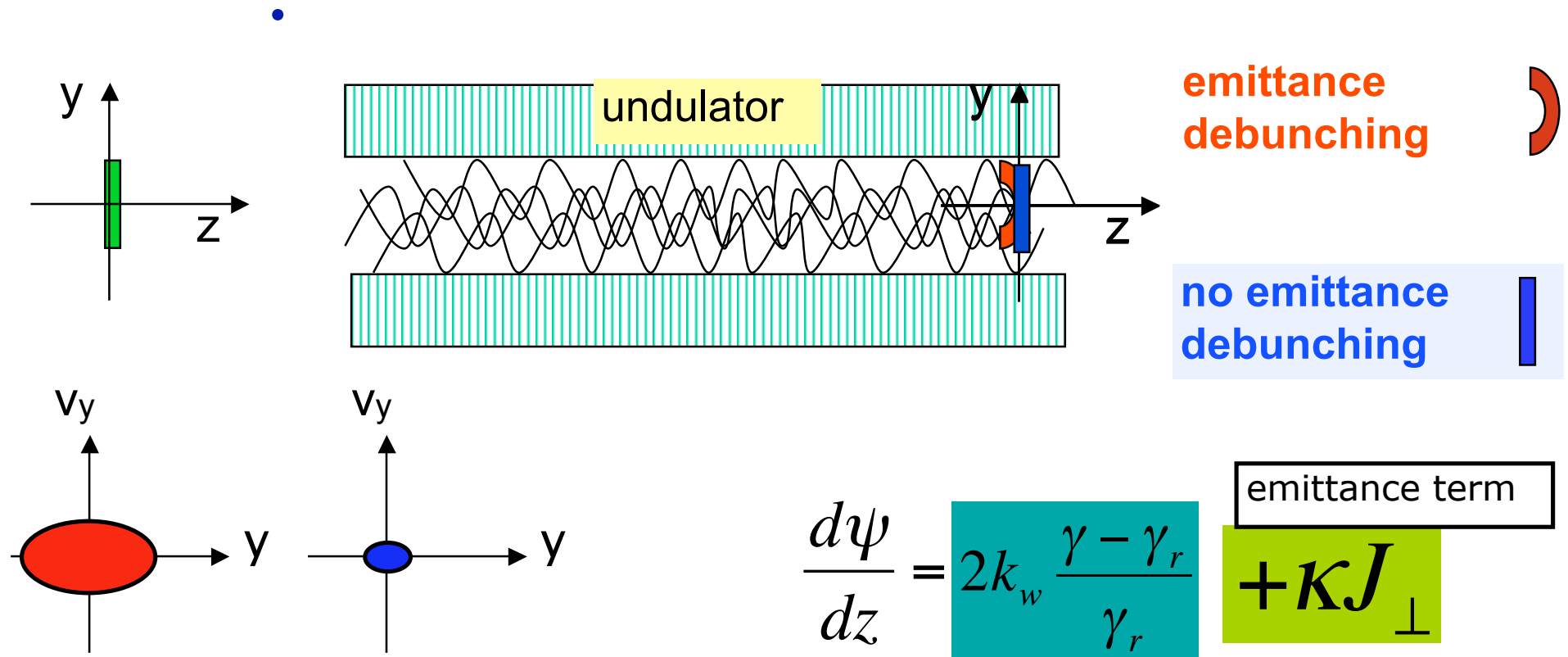
$$\lambda_s = \lambda_w \frac{1 + \gamma^2 \beta_{\perp}^2}{2\gamma^2}$$





FEL unstable when all electrons have initially ~same parallel velocity

*Transverse oscillations mess this up.*

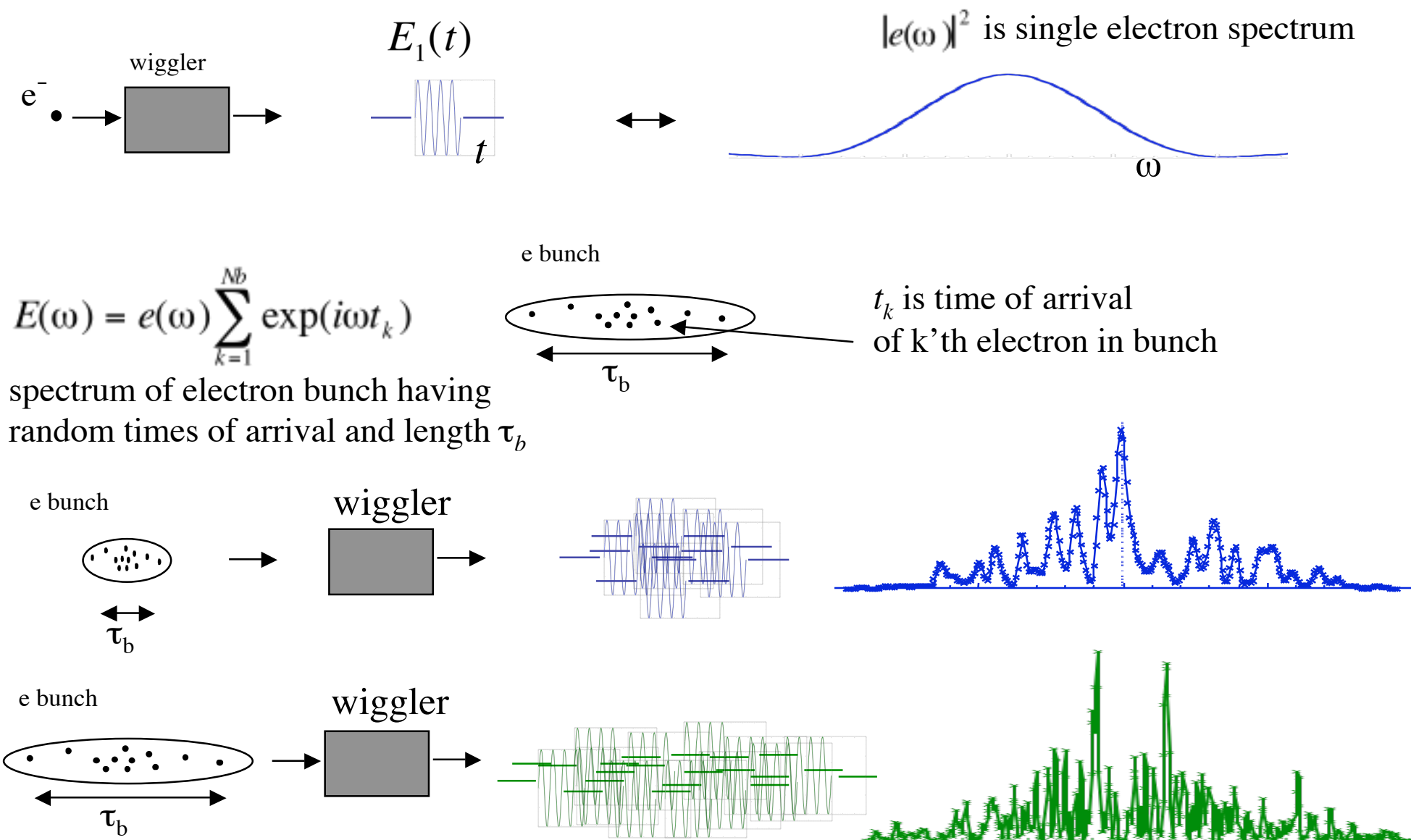


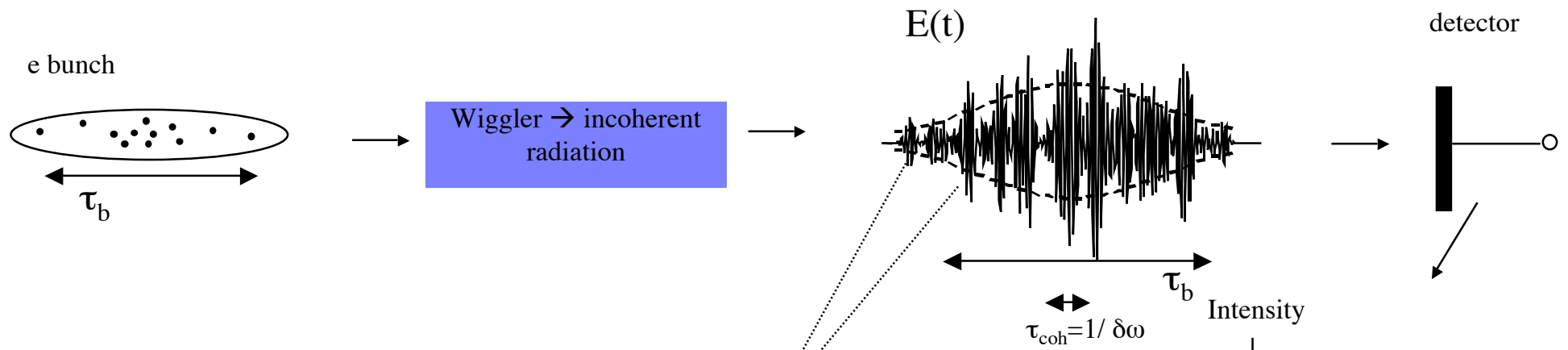
- Emittance requirement in FEL is hard to satisfy at short wavelengths

We are limited by our inability to make high quality beams

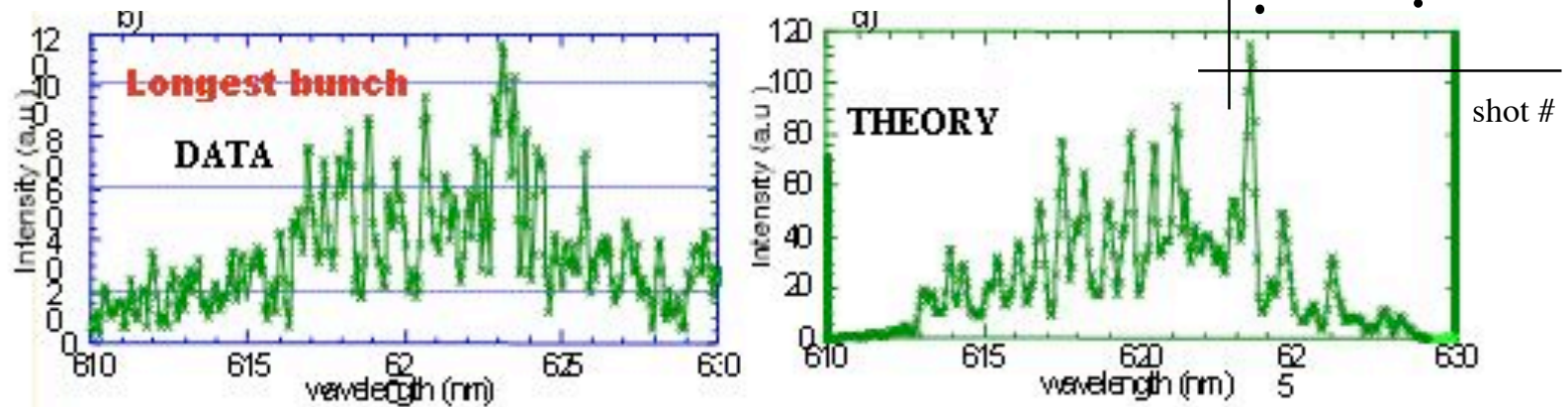


# Single shot noise spectrum contains spikes of width $1/\tau_b$





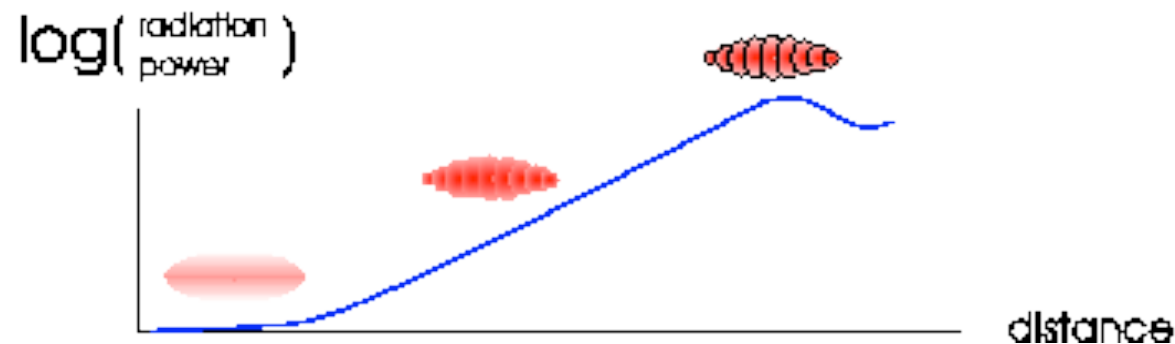
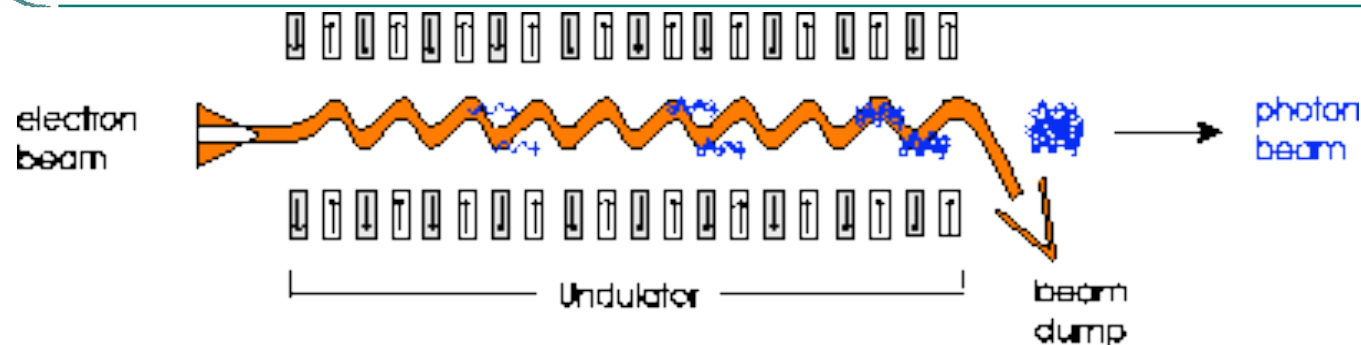
Single pass synchrotron radiation spectrum (Catrivas, et al, @BNL/ATF)



This is the spectrum from which SASE starts---with obvious noise issues and timing jitter.

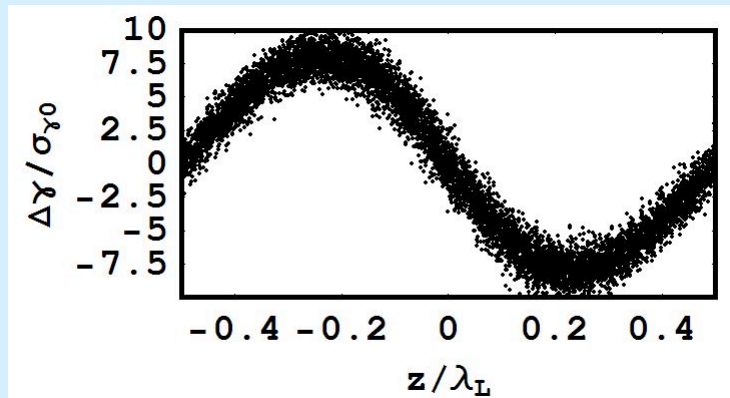
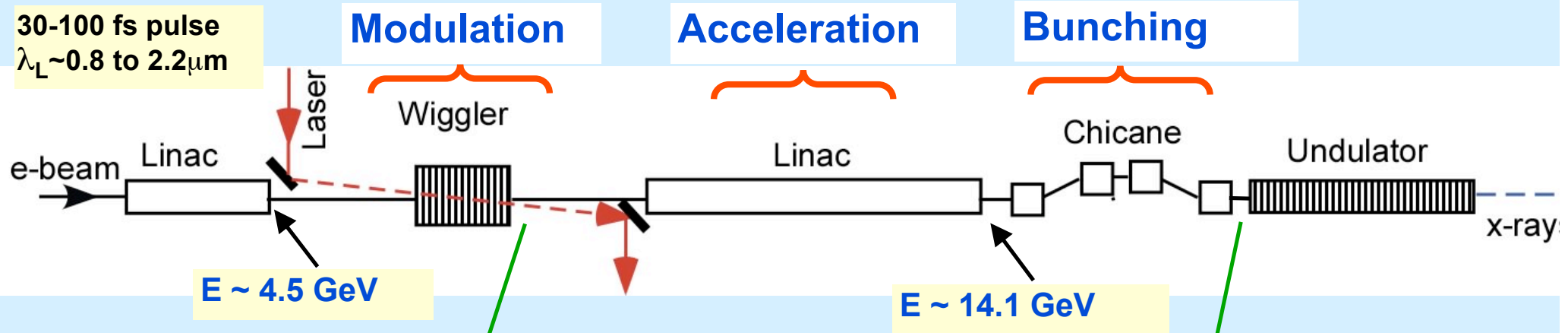


# SASE FEL: amplification of fluctuations

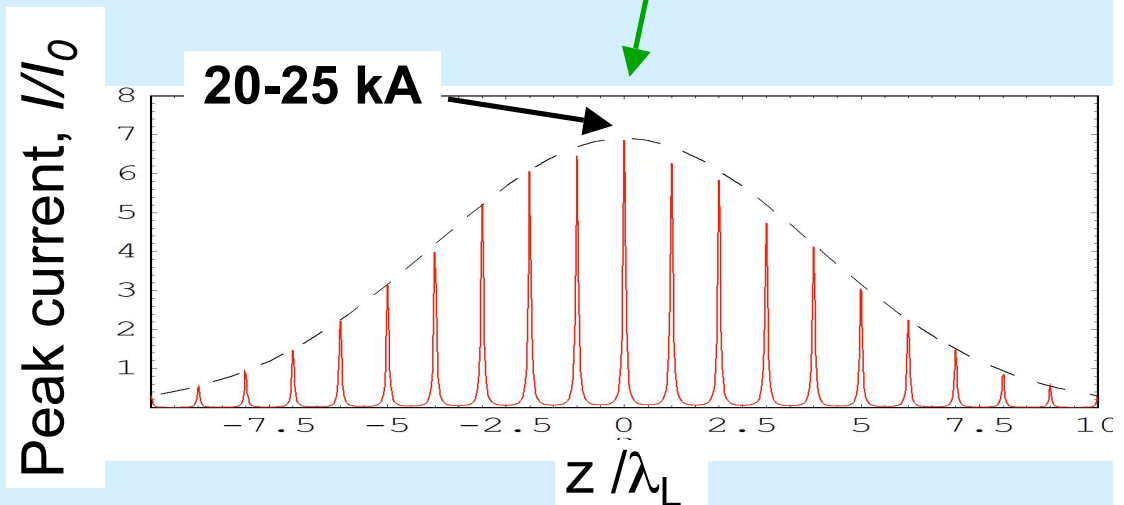


SASE spectrum and temporal shape has spikes--  
poor longitudinal coherence

# ESASE - Enhanced Self Amplified Spontaneous Emission FEL



One optical cycle

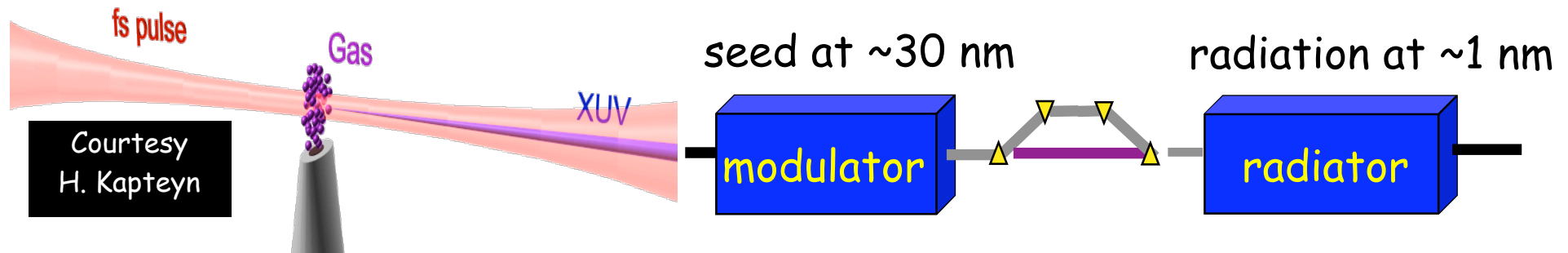


Electron beam  
after dispersive  
bunching

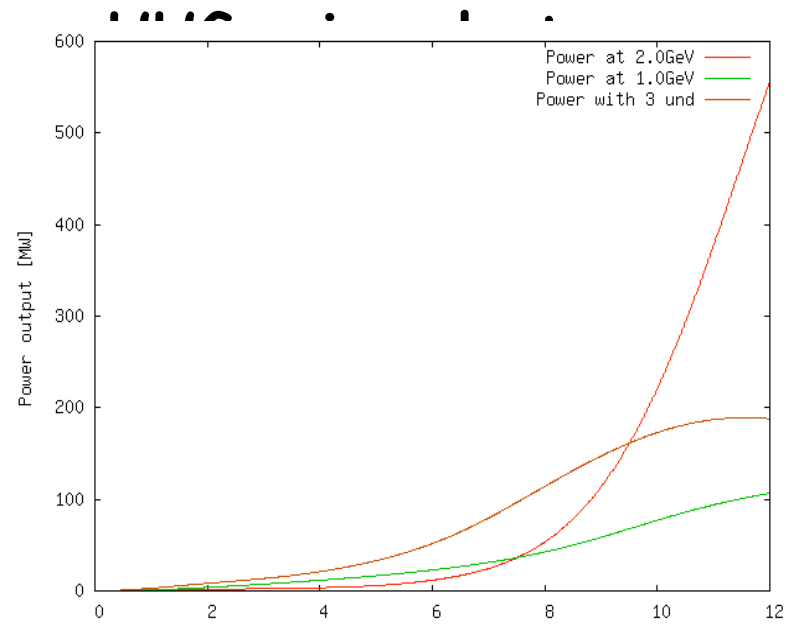
- Laser peak power  $\sim 10 \text{ GW}$  ("easy")
- Short wiggler,  $\sim 10$  periods

# Laser-plasma soft x-ray seed for FEL

- Reduce undulator length by seeding at short wavelength, using fewer stages of harmonic generation in the FEL

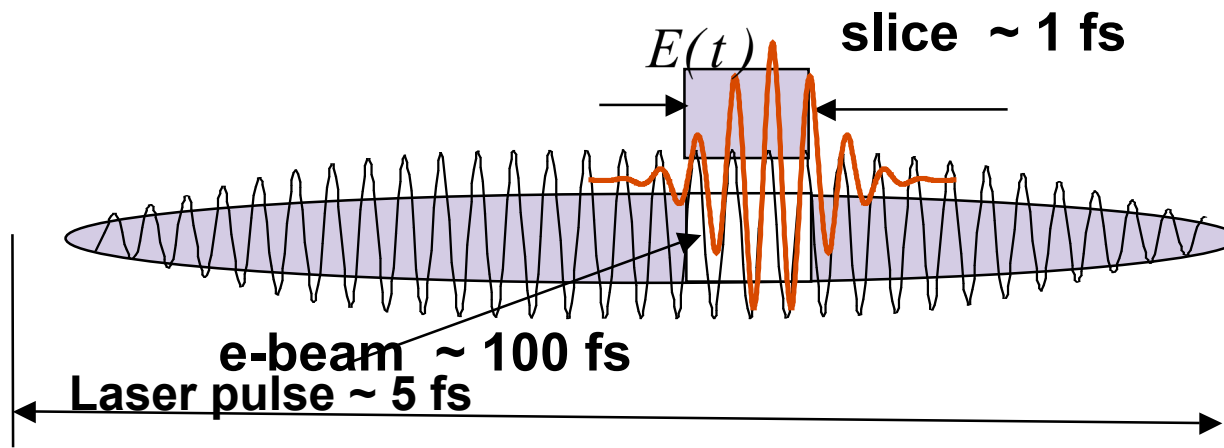


HHG in gas filled capillary  
producing seed pulse for  
energy modulation of electrons





# Lasers manipulate longitudinal phase space during interaction in wiggler



Harmonic cascade seed

This cartoon is realized by manipulation of beam phase space with short pulse lasers. The idea is to condition and select specific slices of electrons to radiate differently (in direction, frequency, intensity, *etc.*). *For synchrotron sources this has already been accomplished:* Zholents & Zolotarev (1996); Schoenlein, et al, 2000; Khan, Part. Acc. Conf. 2005. For FEL see Zholents et al (2003-2007)





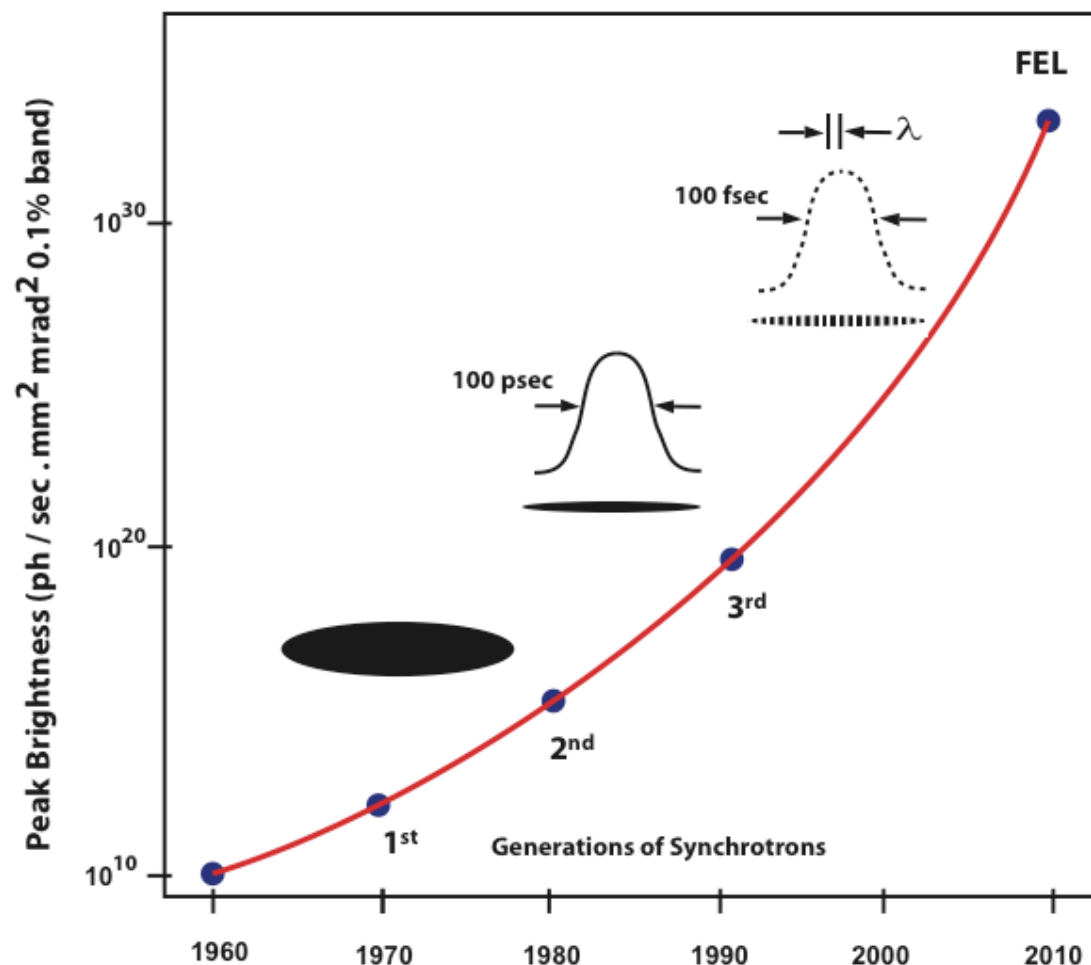
# Evolution of synchrotron radiation sources

Future FELs may have

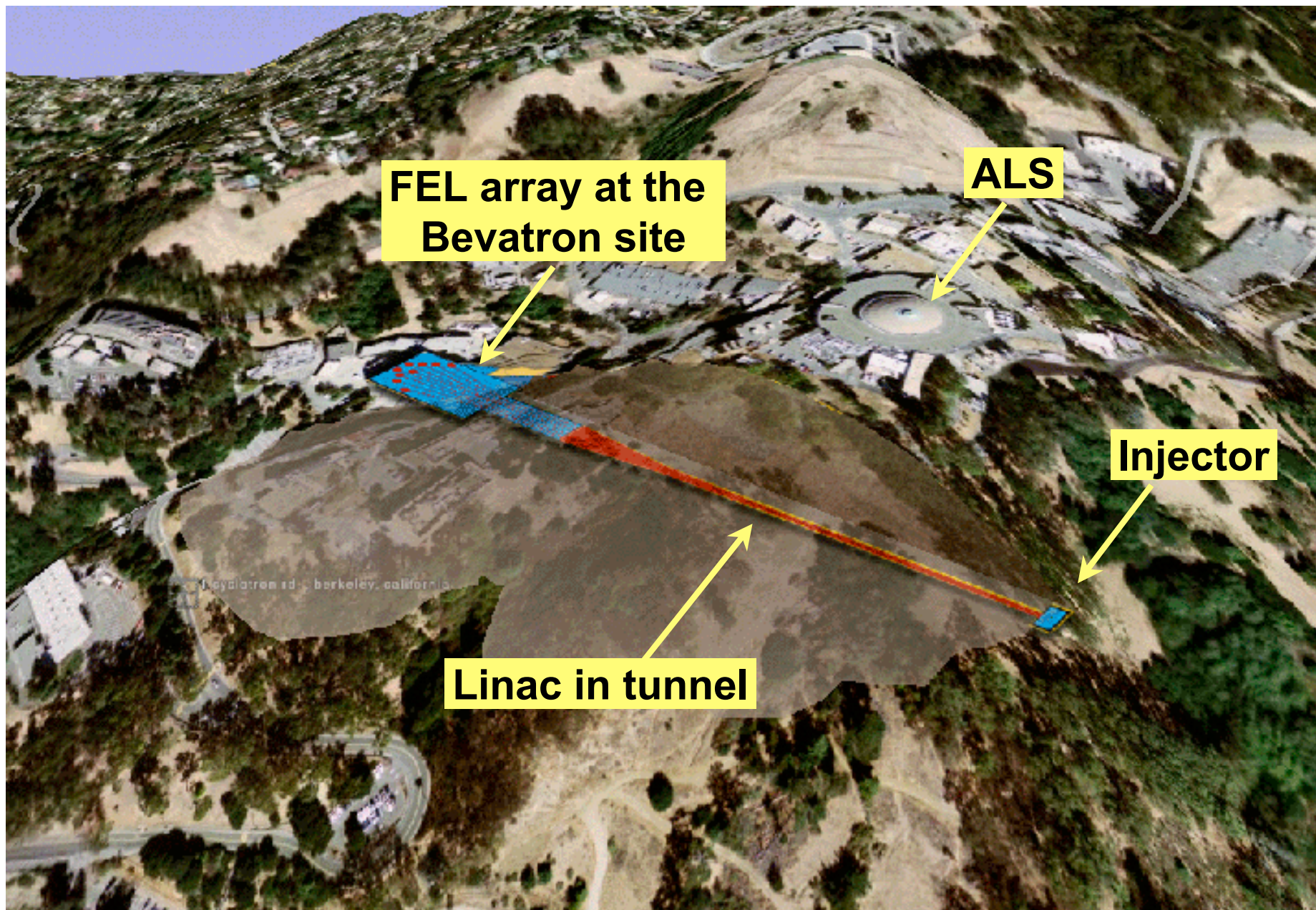
- Energy recovery (ERL)
- Superconducting RF
- High gradient RF
- Optical manipulation of phase space
- Harmonic cascades instead of SASE
- Beam Conditioning

To achieve:

- High average flux
- High peak power
- Temporal coherence
- Spatial coherence
- Attosecond pulses
- Synchronization



# Vision for a future LBNL light source





## Summary: What drives X-ray FELs towards large energy electron beams?

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1. Coherent emission--bunching at X-ray wavelengths
2. Limits on our ability to create and propagate high brightness electron beams
3. Limits on our ability to build short wavelength wigglers





# Plasma-based Accelerators

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- Electron Beams
- Ion Beams

Facilitated by the  
enormous progress in  
laser performance

Advantages: compact, synchronized to laser, short pulse

Disadvantages: hard to measure, jitter, energy spread,...

## ION ENERGIES PRODUCED BY LASER GIANT PULSE

William I. Linlor<sup>1</sup>Hughes Research Laboratories  
Malibu, California*(Received 15 October 1963; in final form 19 November 1963)*

Ion energies of  $\sim 1,000$  eV have been produced by the action of a single "giant pulse" from a ruby laser.

The delivered energy was about 0.2 J in a pulse having full width at half maximum of about 40 nsec. The peak power was 5.4 MW, as measured with a Korad photodiode PDS-20-1C; all pulses were within 10% of this value. The area of the focal spot is not well known; approximate measurements indicate  $10^{-3}$  cm<sup>2</sup>. Energy was determined by the time of flight of the ions over a path of 4.3 cm, and ranged from 0.5  $\mu$ sec for carbon to 1.2  $\mu$ sec for lead.

The targets were in a system at  $10^{-6}$  Torr prior to the laser burst. Within the vacuum system were mounted a lens of focal length 67 mm, a target plate on which the laser beam was focused, and a copper collector plate 3.1 cm o.d. with a 0.64 cm-diam hole to transmit the laser beam. Collector and target plate biases of -23 and -20 V added negligible energy to the ions in comparison with their thermal energy. As indicated in Fig. 1, resistors connected the collector and target to ground. The potentials

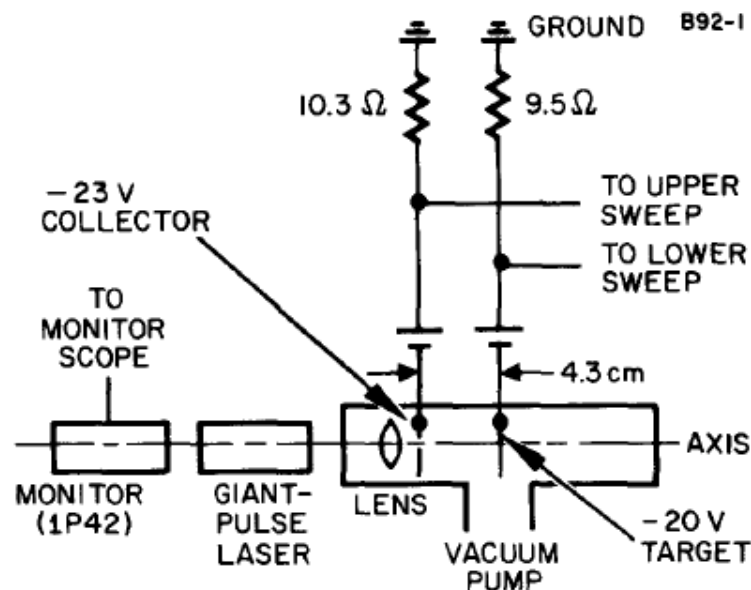
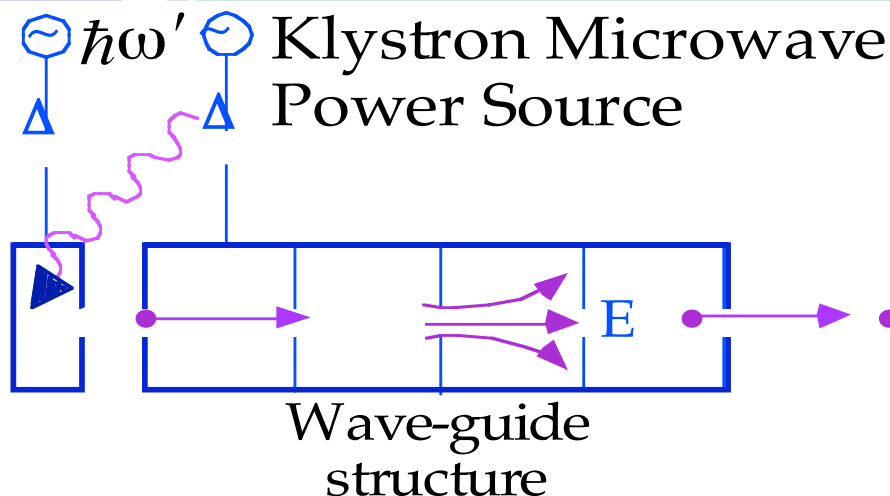


Fig. 1. Experimental system. Laser beam passed through hole in collector, and was focused on the target. Giant pulse was timed by monitor and by flow of electrons from target. System pressure before burst was  $10^{-6}$  Torr.



# Plasma-based Electron Linac



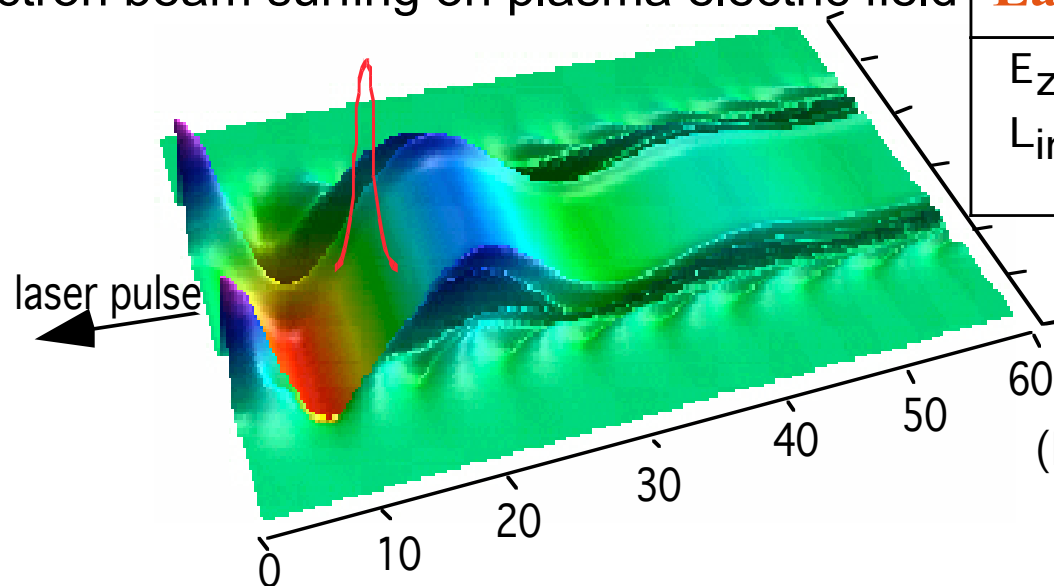
## Conventional Linac

$E_z : 10 - 200 \text{ MV/m}$

$L_{\text{int}} : \text{km's}$

$$W = e E_z L_{\text{int}}$$

Electron beam surfing on plasma electric field

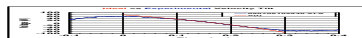


## Laser driven plasma based linac

$E_z : 10 - 100 \text{ GV/m}$

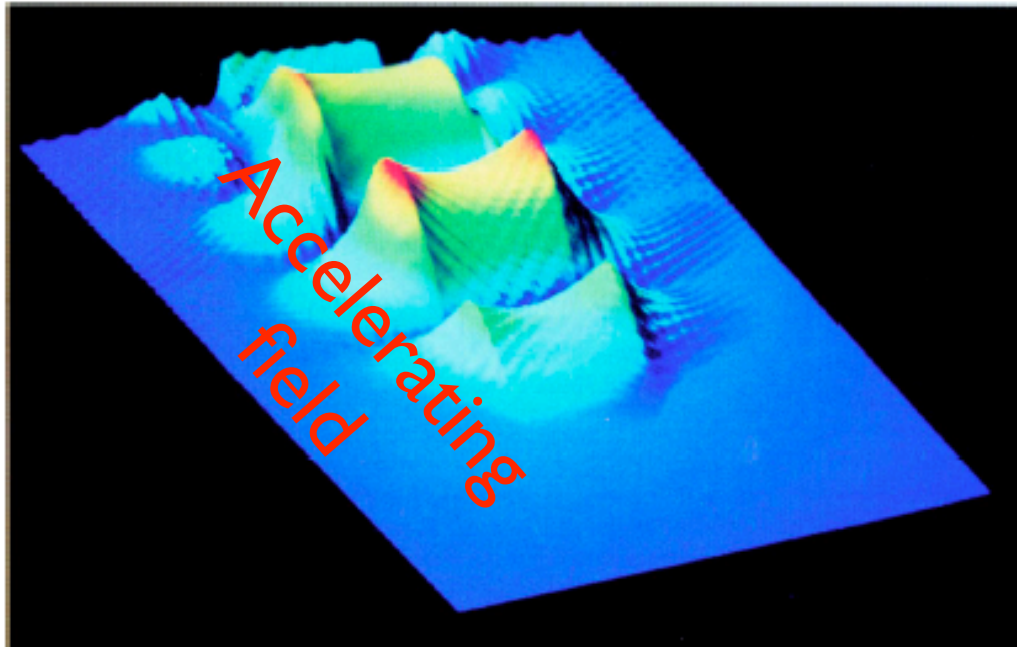
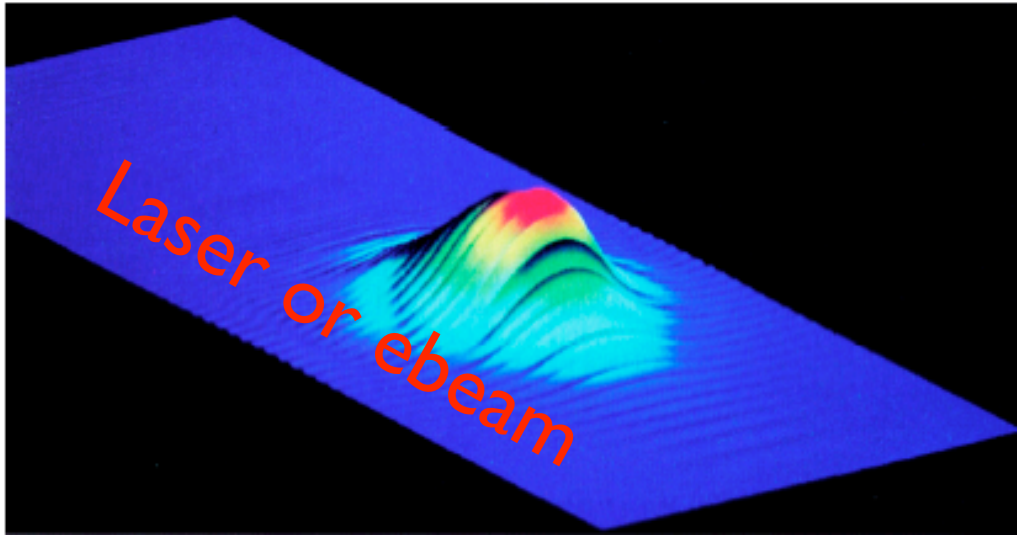
$L_{\text{int}} : \text{laser diffraction length}$

(B. Shadwick, UCB/CBP)

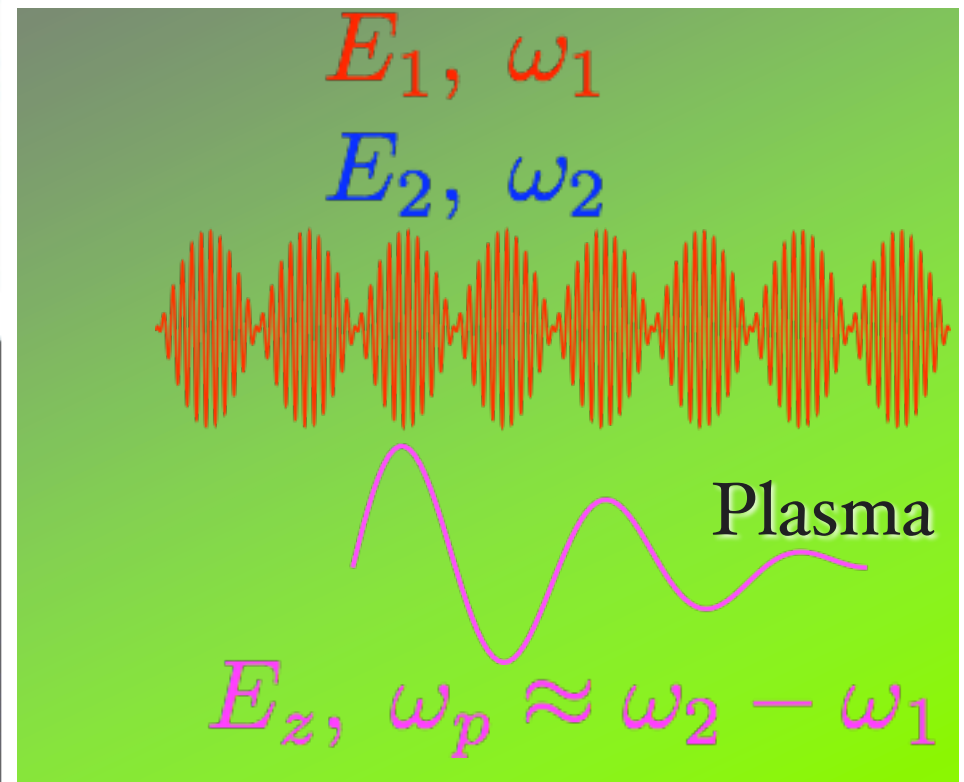




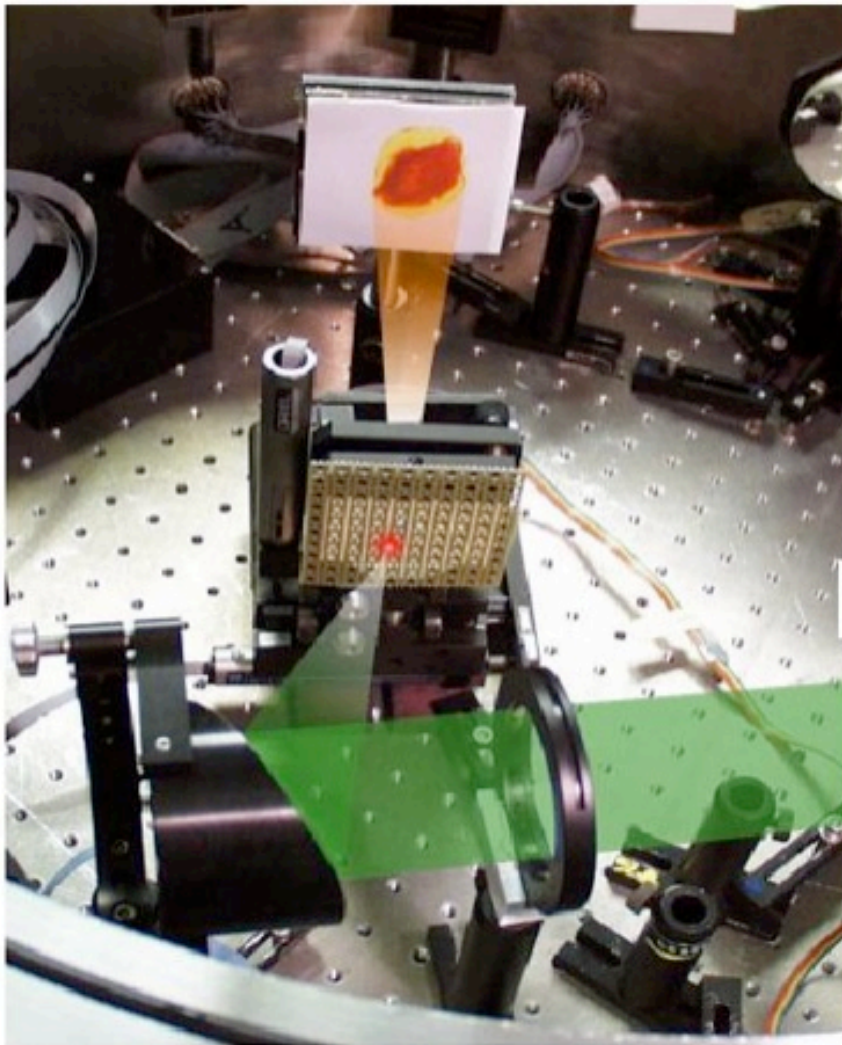
# Creation of Accelerating Structures in Plasmas: Femtosecond Engineering Wakefield



Beatwave



# A Beam of MeV Protons



- $a_0 = 3.0$
- Cone angle =  $40^\circ$
- Always normal to the target
- Front side origin
- $2\pi$  mm-mrad
- $E \sim 10$  GeV/cm
- $N > 10^{10}$  p
- $J = 10^8$  A/cm<sup>2</sup>

A. Maksimchuk, K. Flippo, D. Umstadter, V.Y Bychenkov, *Phys. Rev. Lett.* **84**, 4108 (2000).

# A laser-driven ion accelerator (cartoon)



from supplementary material: B. M. Hegelich, B. J. Albright, J. Cobble, K. Flippo, S. Letzring, M. Paffett, H. R. ...  
*Nature* **439**, 441-444 (26 January 2006)

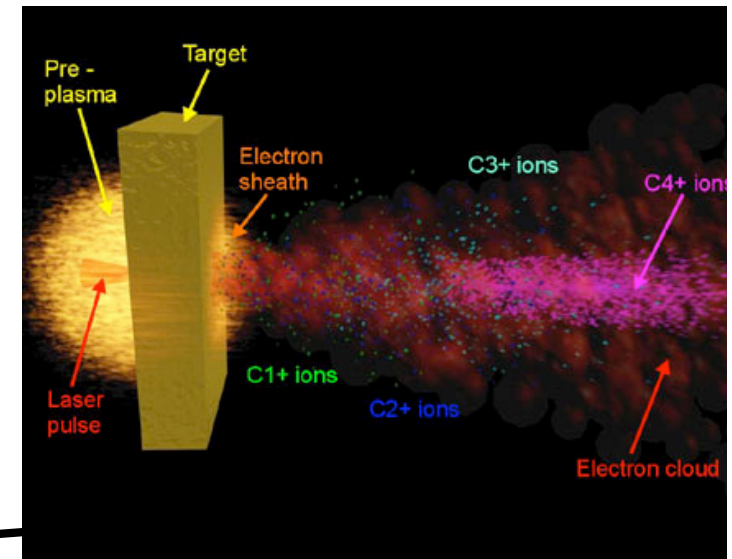
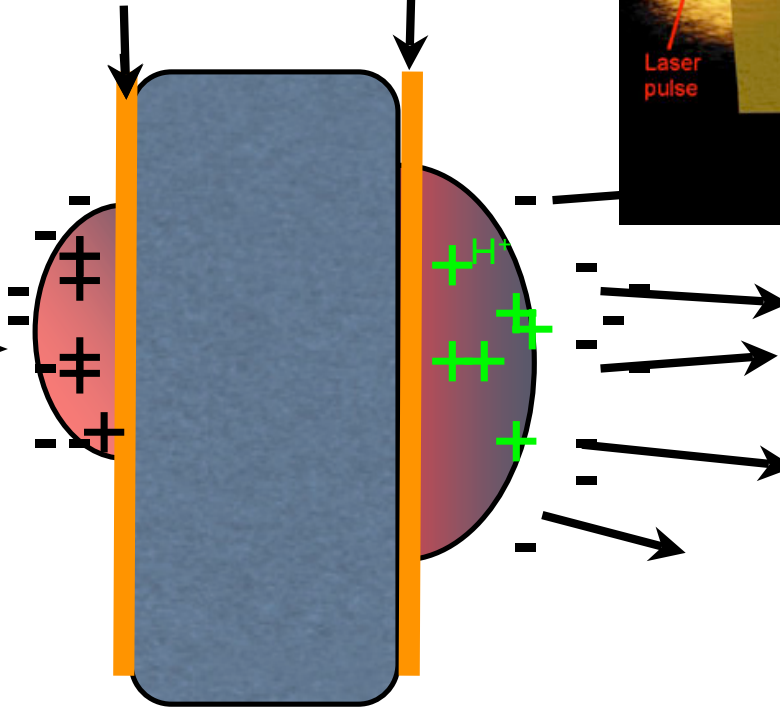
# Ion Acceleration from laser-solid

Applications  
 Spallation source  
 plasma probe  
 fast ignitor  
 wdm  
 high energy density physics

Laser:  
 $P > 10 \text{ TW}$   
 $10^{18} \text{ W/cm}^2$

Contaminants ( $\text{H}_2\text{O}$ )

Surface prep



Heglich et al  
 Nature 2006

Properly prepared and shaped target can accelerate ions

Gitomer et al, 1986

Sentoku et al. (2003)  
 Hegelich et al. (2002)

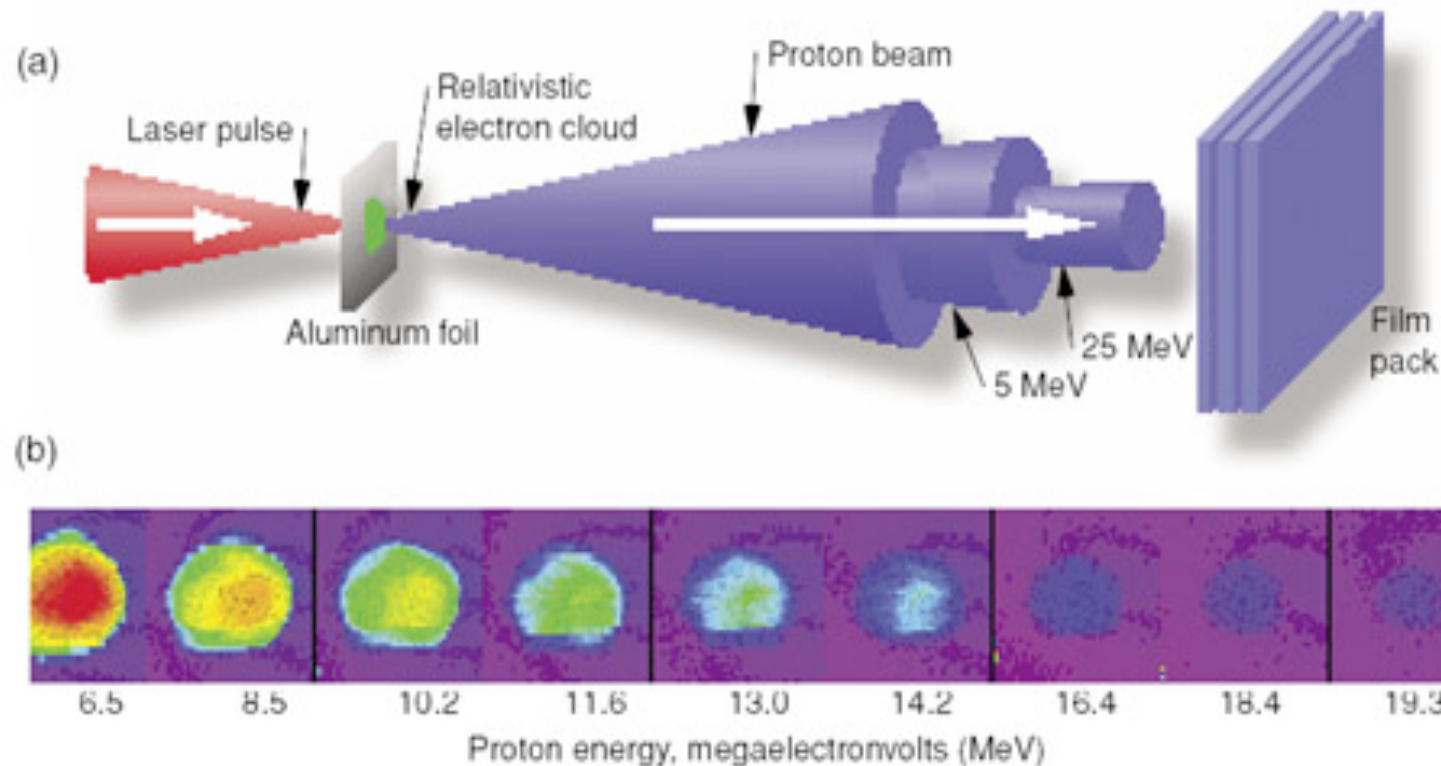
Snavely et al. (2000)  
 Fuchs et al 2005, Allen et al (2005)





# Laser Acceleration of Ions

P. K. Patel, et al



- Protons from JanUSP --10J, 100fs
- High flux (1-2% of laser energy)
- Exponential distribution ( $kT \sim 2-3\text{MeV}$ )
- High peak energy ( $< \sim 25\text{MeV}$ )
- Strongly collimated (1-20)
- few ps pulse length



# References

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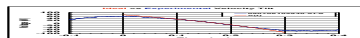
## Basic accelerator physics

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- Particle Accelerator Physics, [Helmut Wiedemann](#), [Springer-Verlag](#), Berlin, 1993.
- Principles of Charged Particle Acceleration, Stanley Humphries, Jr., [John Wiley & Sons](#), New York, 1986.
- The Principles of Circular Accelerators and Storage Rings, Philip J. Bryant and Kjell Johnsen, [John Wiley & Sons](#), New York, 1984.
- Theory and Design of Charged Particle Beams, [Martin Reiser](#), [John Wiley & Sons](#), New York, 1990.

## With more emphasis on collective effects

- Physics of Collective Beam Instabilities in High Energy Accelerators [Alexander Wu Chao](#), [Clarendon Press](#), Oxford, 1983.
- The Physics of Charged Particle Beams, J.D. Lawson, [Clarendon Press](#), Oxford, 1988.
- Charged Particle Beams, Stanley Humphries, Jr., [John Wiley & Sons](#), New York, 1990.
- Intense Charged Particle Beams, R. B. Miller, [Plenum](#), New York, 1982.

**Physics of Intense Charged Particle Beams in High Energy Accelerators** by Ronald C. Davidson and Hong Qin  
**Physics of Nonneutral Plasmas** by Ronald C. Davidson





# Conclusion

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- Ion beams and FEL X-ray sources are being developed for, among others, warm dense matter applications
- Electron beams for X-ray FELs: high brightness and GeV energies--large facilities with CSR and other intensity limits
- Plasma acceleration-- 1-100GV/m fields, compact source, femtosecond bunch lengths, beam brightness, stability and dark current limits; high average and peak powers, cost,
- Ion acceleration-- high gradients, injector for conventional linac, WDM/HEDP/fast ignition/probing studies; no need for low beta rf structure; peak and average laser power, energy spread, emittance, staging, diagnostics for beam.
- MANY THINGS NOT DISCUSSED--but more on ION beam drivers in talks later today.